

Operational Risk: EVT Models

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FRB Boston 14-16 Nov. 2001

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- Introduction (The Problem)
- Methodology Survey
- Extreme Value Theory
- Example
- Assumptions and Issues
- Summary





• What is the maximum amount of loss due to operational risk that can be expected in a specific business unit over a period of one year at a very high confidence level (e.g. 99%) ?





- Business unit with no market or credit risk.
- Processes composed of people, systems, and infrastructure.
- Business model is based on earning fees for services.
- Value is added to individual transactions.





- Factor approach
 - Identify key indicators and relationships to losses.
 - Use a factor model to calculate the capital requirement directly, (e.g. 12% of income).
- Delta approach
 - Calculate volatility of profits using error propagation technique that relates volatility of profits to volatility of key indicators using sensitivities.
 - Choose a factor on profit volatility based on distributional assumption (normal or lognormal) and required confidence interval, plus a 'fudge' factor.





• Loss model

- Record losses made and fit a parametric distribution to their severity and one to their frequency.
- Use simulation to create cumulative loss distribution for the period based on frequency and severity.
- Choose quantile of resulting distribution, plus a 'fudge' factor





- Factor model that is predictive.
 - Uses measure at hand and linear relationship to predicts measure not at hand.

$$\Delta p = \frac{\partial p}{\partial f} \Delta f$$

- Theory
 - Partial differential equations (PDE's).
- Example
 - Change in interest rate used to predict change in bond price.





- Assumption
 - Causal relationship between measured indicator and predicted measure.
 - Linear relationship (approximated)
- Advantages
 - Predictive
 - Understandable
- Disadvantages
 - Factor interactions
 - Non-linear relationships
 - Unknown factors





• Use historical results to predict future values of a measurement based on an intrinsic regularity and symmetry of underlying system.

• Theory
$$x_{t+1} = \Phi\{x_{t-n}, \dots, x_t\}$$

- Statistical distributions
- Example
 - Yearly claims loss of automobile insurance business for defined set of policy characteristics.



Loss Models



- Assumptions
 - Underlying regularity and symmetry are known and stable.
- Advantages
 - Allows prediction without understanding causes.
 - Large samples tend toward a regularity and symmetry.
- Disadvantages
 - Irregularity and shocks to the system.
 - Not easily influenced because no known causes.
 - 'Post-predictor' that is insensitive to outliers.



Advanced Models -- Causal Models

- Causal Models
 - Advantages of factor model
 - Non-linear relationships
 - Mitigates interrelationships of factors





- Loss Model
 - Uses one of the extreme value distributions for severity distribution.
 - Fits distribution based on extreme events only.
- Generalized Pareto Distribution (GPD)
 - Fits the excess losses above a threshold.

$$GPD(x) = \left((1 + \xi) \frac{x - threshold}{\beta} \right)^{-\frac{1}{\xi}}$$





Data:

Analysis:

Theory:

Application:

Only need large losses (not all losses).

Not influenced by volume of small losses.

Well-founded theory beginning with Fisher-Tippet.

Widely applied in physical sciences (damns, dykes, reliability).





- Uses the Delta factor model for high frequency, low severity losses.
- Uses EVT loss model for low frequency, high severity losses.
- Combines the two approaches using the threshold value for large losses.



Delta-EVTTM Combination Methodology

• Combines Delta and EVT to link performance of the business to the losses and provide a built-in validation of capital charges

capital charges.







- Business Unit Description
 - Profit center in financial services
 - No market or credit risk
- Problem
 - What is the maximum amount of loss due to operational risk that can be expected in a this business unit over a period of one year at a very high confidence level (e.g. 99%)?





Business Process					
Transactions/day	1 000				
$\frac{11}{11} \frac{11}{11} 11$	1,000				
Transactions/year (*)	260,000				
Average transaction value	200,000 €				
Transaction margin	100 bp				
Transaction net value	200 €				
Net per year	52,000,000 €				
Proposed capital ratio	12%				
Capital Required	6,240,000 €				

(1) 260 days/year





Delta Loss						
Loss rate	3%					
Loss transactions/day	30					
Loss transactions/year	7,800					
Average loss/loss transaction	200	€				
Average total loss/year	1,560,000	€				
But: And actual year's loss is:	σ = 500 5,529,860	€ (~lognormal)				



Poisson-Lognormal Simulation



Poisson-Lognormal Simulation



Run



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All Transaction Losses for Year





Large Losses



		Amount		
ID	Date	('000)	Loss	
1	01/01/98	-35.1	35	
2	01/19/98	-40.0	40	
3	01/30/98	-55.0	55	
4	02/11/98	-80.9	81	
5	02/12/98	-508.0	508	
6	02/17/98	-3.5	4	
7	03/18/98	-48.8	49	
8	03/20/98	-12.0	12	
9	03/27/98	-168.9	169	
10	03/27/98	-98.0	98	
11	04/07/98	-128.0	128	
12	06/01/98	-21.6	22	
13	06/11/98	-100.0	100	
14	07/01/98	-770.0	770	
15	07/24/98	-142.0	142	
16	08/18/98	-61.5	62	
17	08/30/98	-129.4	129	
18	10/05/98	-1450.0	1450	
19	10/12/98	-30.0	30	
20	10/15/98	-17.0	17	
21	10/22/98	-8.0	8	
22	11/30/98	-12.0	12	
23	12/28/98	-50.0	50	



Total of large losses is €3,969,700











Summary of Yearly Losses in Business Unit							
at High Confidence Levels							
	In Control		Out of Control				
	(Poisson-Lognormal)		(Poisson-GPD)		Total		
Quantile	events	loss	events	loss	events	loss	
90%	7,911	1,757,224	30	2,557,100	7,941	4,314,324	
95%	7,940	1,771,004	32	3,262,250	7,972	5,033,254	
99%	8,020	1,816,982	35	7,846,340	8,055	9,663,322	
99.9%	8,068	1,834,619	39	14,381,519	8,107	16,216,138	

(Factor model using 12% of income was €6,240,000)





- Delta Model
 - There is little affect from the mean loss figure.
 Most of the information is found in the volatility (sigma). The calculation of the volatility of the losses does not need large losses (or any losses), but needs to be validated using a sample of losses.
 - Is not affected by large losses (or any previous losses for that matter).





- Lognormal Loss Model
 - Contributes little to the delta methodology when there is a large sample of losses available, since most of the information is present in the volatility of the losses.
 - Could be used for validation of delta method, or reduced to a small sample size.
 - Is not affected by the inclusion of large losses when the sample size is large.





- EVT Loss Model
 - Captures the effect of large losses and shows an order of magnitude difference in the use of a delta or lognormal loss model when large losses are present.
 - Has little affect on the average loss or loss
 volatility, and does not account for losses below
 the threshold.





- A complete loss database is not required to develop a delta model or parametric loss model when a large number of losses are available and large losses are excluded from the model.
- EVT models are needed to handle situations where large losses are present (e.g. losses that lie outside any reasonable confidence limit of the delta or parametric loss model).





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